## $\mathrm{P}_{\mathrm{T}} \mathrm{CT}_{\mathrm{E}} \mathrm{X}:$ Macros for Drawing Pretures

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## Overview

In the preface to The TEXbook, Knuth describes TEX as a "typesetting system intended for the creation of beautiful books - and especially for books that contain a lot of mathematics". $\mathrm{PICT}_{\mathrm{E}} \mathrm{X}$ is a collection of $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ macros by means of which $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ users can easily instruct $T_{E X}$ to typeset beautiful pictures as a part of their books - and especially mathematical figures, such as the one below.

Figure 1. Density $\mathfrak{a}$ and distribution function $\mathfrak{A}$ of the arc sine distribution. The shaded area under the graph of $\mathfrak{a}$ is $\mathfrak{A}(\beta)-\mathfrak{A l}(\alpha)$.

$$
\begin{gathered}
\text { Density } \\
\mathfrak{a}(t)=1 /(\pi \sqrt{t(1-t)})
\end{gathered}
$$

Distribution function



That figure and the others in this article illustrate the main things you can do with $\mathrm{P}_{\mathrm{I}} \mathrm{CT}_{\mathrm{E}} \mathrm{X}$ : place text into a PICture; construct $x$ and $y$ axes with tick marks, tick labels, and axis labels; draw rectangles and other things made out of horizontal and vertical rules; draw straight lines and curves (without recourse to special fonts); use line fills that can be solid, dotted, 「dashed, or otherwise'; and shade regions. In addition to these "primitive" graphics capabilities, $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}_{\mathrm{E}}$ provides some "upper" level commands for drawing things like bar graphs, histograms, arrows, circles, and ellipses. Using TEX's powerful macro facilities, you can readily create other upper level commands that are tailored to your specific needs.
$\mathrm{P}_{\mathrm{T}} \mathrm{CT}_{\mathrm{E}} \mathrm{X}$ has these advantages: (1) Figures become an integral part of the typesetting process. You can avoid having to leave the proper amount of space in your document for material that has to be created on some external device and later stripped into the finished product. (2) All of $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ 's formatting capabilities are available for annotating your figures. In addition, that annotation will be

Figure 2. A segment of a complex flow chart.

done in the same fonts that you're using in the rest of your document. (3) Just as $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ is machine independent, so too is $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}_{\mathrm{E}}$. It doesn't matter whether you're working on a PC or mainframe computer. (4) Since typeset figures are embedded in the dvi file along with the rest of your document, all the advantages of $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ 's device independent output accrue to them. In particular, you can revise away to your heart's content on your local system until your PTCtures look just the way you want them to, and then you can have the final copy elegantly printed on a high resolution output device. (5) $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}_{\mathrm{E}}$ can be extended using $\mathrm{T}_{\mathrm{EX}}$ 's macro facilities, and can be used with $\mathrm{IAT}_{\mathrm{E}} \mathrm{X}$.

On the other hand, $\mathrm{PTCT}_{\mathrm{T}} \mathrm{X}$ has several limitations: (1) $\mathrm{P}_{\mathrm{I}} C T_{E X}$ was expressly designed to facilitate the construction of pictures such as Figure 1. It simply is not the right tool for producing illustrations such as the lions that grace the title pages of The $T_{E} X b o o k$. (2) Within the realm of mathematical figures, $\mathrm{PICTEX}_{\mathrm{I}}$ itself doesn't make 3D pictures or other complex things. Considering that $T_{E X}$ provides fewer arithmetic capabilities than the simplest pocket calculator, that would be asking for too much. However $\mathrm{PICT}_{\mathrm{E}} \mathrm{X}$ can be used as an interface between $\mathrm{TEX}_{\mathrm{E}}$ and a sophisticated graphics program. For example, Figure 2 was set using Fig and a Fig-to- $\mathrm{P}_{\mathrm{I}} \mathrm{CTEX}_{E}$ converter developed by Micah Beck. (3) PTCTEX takes a while to draw a PTCture. Figure 1 initially took 30 seconds on a Sun $3 / 60$, the bulk of the time going into producing the two curves. In subsequent drafts $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}$ used a special routine to replot the curves and did the whole P PCture in 10 seconds. (By contrast, running on a Sun $3 / 60, \mathrm{TEX}$ processes a page of "straight

Figure 3. Number of words Shakespeare used exactly $n$ times, for $n=1$ to 100 by 1 .

text" in about 1 second.) (4) PTCtures take up a sizable amount of computer memory. A large $P_{\mathrm{T}} \mathrm{Cture}$ with several curves will exceed the capacity of a standard version of TEX. This difficulty can be circumvented by using a larger version of $\mathrm{TEX}_{\mathrm{E}} \mathrm{X}$, such as that developed by Bart Childs et al. (See page 122.)

The $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}$ manual contains detailed instructions on the use of the $P_{I} C_{E} X$ macros, with many examples and exercises, along with a command summary and index. The manual is about 90 pages long. Both the macros and the manual may be obtained from TUG.

The next section of this article has some examples showing how one goes about drawing a PICture. The final section has an example showing how $\mathrm{P}_{\mathrm{C}} \mathrm{CTEX}$ can be extended via TEX's macro facilities.

## Drawing PICtures

Table 1 lists the code that was used to construct Figure 3, in which the common logarithm of the number of words Shakespeare used exactly $n$ times is graphed versus $n$ for $n=1,2, \ldots, 100$. In tabular form the data are as follows:

| $n$ | $\nu_{n}=$number of words <br> used $n$ times | $\lambda_{n}=\log _{10}\left(\nu_{n}\right)$ |
| ---: | :---: | :---: |
| 1 | 14,376 | 4.1576 |
| 2 | 4,343 | 3.6378 |
| 3 | 2,292 | 3.3602 |
| $\vdots$ | $\vdots$ | $\vdots$ |
| 99 | 7 | 1.1761 |
| 100 | 5 | 0.6990 |

Figure 3 has $n$ on the horizontal ( $x$ ) axis, and $\lambda_{n}$ on the vertical ( $y$ ) axis.

Table 1. $P_{I} C T E X$ commands for Figure 3. (The line numbers are not part of the commands.)

```
\beginpicture
\setcoordinatesystem units <.02in,.4in>
\multiput {$\scriptstyle\circ$} at
    14.1576 2 3.6378 3 3.3602
    43.1652 5 3.0183 6 2.9227
    (additional coordinates omitted here)
    951.0000 96 1.0000 97 1.1761
    98 0.8451 99 0.8451 100 0.6990/
\put {$\longleftarrow
    \vcenter{\hsize=100pt \raggedright
    \eightpoint \noindent
    Shakespeare used 14,376 words exactly
    once.}$} [1] <4pt,0pt> at 1 4.1576
\setplotarea x from 0 to 100,
        y from 0 to 4.301
\axis bottom
    label {Frequency $n$ of usage}
    ticks numbered from 0 to 100 by 20
            short unlabeled quantity 11 /
\axis left shiftedto x=-5
    label {\stack
        {N,u,m,b,e,r,,,o,f, ,,w,o,r,d,s}}
    ticks logged
        numbered at 1 10 100 1000 10000 /
        unlabeled short from 2 to 9 by 1
            from 20 to 90 by 10
            from 200 to 900 by }10
            from 2000 to 9000 by }100
            at 20000 / /
\endpicture
```

Table 1 is largely self-explanatory, since much of the code reads almost like English. However, some remarks are in order: (1) The command on line 2 tells $\mathrm{PTCTEX}_{\mathrm{E}}$ to set up a rectangular coordinate system in which one unit on the $x$ axis has length of .02 inches, and one unit on the $y$ axis has a length of .4 inches. The value .02 was chosen so that a run of 100 units on the $x$ axis would amount to $.02 \times 100=2$ inches, leaving plenty of room in TUGboat's 3 inch column for the $y$ axis structure. (2) The command on lines $3-7$ places small circles at the coordinate points $(1,4.1576), \ldots,(100,0.6990)$. The trailing $\%$, on line 7 informs PTCTEX that the list of coordinate points is exhausted. (3) The option '[1] <4pt, 0 pt$\rangle^{\prime}$ on line 12 to the \put command on line 8 instructs $\mathrm{P}_{\mathrm{T}} \mathrm{CIEX}$ to place the associated text (i.e., the arrow and the \vcentered paragraph) into the $P_{\text {T }}$ Cture with its left edge 4 points to the right of the the designated coordinate $(1,4.1576)$.
(4) $\mathrm{P}_{\mathrm{T}} \mathrm{CT} \mathrm{X}$ draws coordinate axes along the edges of a prespecified rectangular "plot area". The command on lines $13-14$ sets up such a plot area, running from 0 to 100 along the $x$ axis and from 0 to $4.301=\log _{10}(20,000)$ along the $y$ axis. The command on line 15 draws an axis along the bottom edge of this plot area. The analogous command on line 19 creates an axis along the left edge of the plot area; however this axis is subsequently shifted to lie along the line $x=-5$.

Some features of $\mathrm{PICTEX}_{\mathrm{I}}$ that emerged in the preceding example merit further discussion. The coordinate system is a key element of any PTCture, since it governs the placement of everything that's put into that $P_{\text {ICture }}$ You can set and reset the coordinate system at will, moving the location of the origin and changing the lengths of the $x$ and $y$ units; this facilitates work on $\mathrm{P}_{\mathrm{T}} \mathrm{Ctures}$ like Figure 1 having several components. $\mathrm{P}_{\mathrm{T}} \mathrm{TTEX}_{\mathrm{E}}$ 's $\backslash$ put command and its relatives have options that make it easy to specify exactly how an object should be positioned relative to a given coordinate. You can choose between various horizontal (centered, left, right) and vertical (centered, above, below, baseline) orientations, and you can offset objects horizontally and vertically by amounts that don't depend on the current coordinate system. \axis is PTCTEX's most versatile command. You can: choose between bottom, left, top, and right axes; freely specify where ticks are to be placed; use any combination of unlabeled, numbered, or user-labeled ticks; have the ticks marks point out from the plot area or into it, or even extend all the way across it; specify axis labels and a plot heading; govern the length and thickness of axes and tick marks; and adjust the spacing between the various components of the graph framework. In general you can fine tune any part of a PICture; a few minor adjustments may make the difference between a figure that is merely presentable and one that is a work of art. One last point: you don't have to prespecify to TEX how much room a $P_{T} C t u r e$ will take up. $P_{T} C_{E X}$ automatically determines the size of a P PCture and passes this information on to $T_{E X}$ so that the $P_{T} C-$ ture can be positioned appropriately in the page layout.

What about lines and curves? PTCIEX has four interpolation modes, two of which are piecewise linear interpolation and piecewise quadratic interpolation. (The other two modes generate histograms and bar graphs.) Moreover, $\mathrm{P}_{\mathrm{I}} \mathrm{CTEX}$ has four modes for line fill: solid, dotted, dashed, and user-specified. Given a list of coordinate points, $\mathrm{P}_{\mathrm{ICTEX}}$ 's $\backslash$ plot command connects those points

Figure 4. Trinomial sample space and probabilities for $m=6$ and $\pi=(1 / 3,1 / 3,1 / 3)$. For nonnegative integers $y_{1}, y_{2}$, and $y_{3}$ summing to $m$, the probability at the point $\left(y_{1}, y_{2}, y_{3}\right)$ is $\frac{m!}{y_{1}!y_{2}!y_{3}!} \pi_{1}^{y_{1}} \pi_{2}^{y_{2}} \pi_{3}^{y_{3}}$. (The $y_{3}$ axis recedes into the plane of the page.)

using the current interpolation and line fill modes. Every option in $\mathrm{PTCTEX}_{\mathrm{T}}$ has a default; the defaults for $\backslash$ plotting are piecewise linear interpolation with solid line fill.

For example, in Figure 4 the edges of the simplex were drawn simply with
\plot $0660 \quad 85 \quad 06$ /
while the $y_{3}$ axis was created with

```
\setdashes
\plot 0 0 8.5 5.3125 /
```

In Figure 1 the left-half of the arc sine density $\mathfrak{a}$ was created by first placing the origin of the coordinate system at the point $t=0.5$ on the horizontal axis, and by then entering

$$
\begin{aligned}
& \text { \setquadratic } \\
& \begin{array}{lllll}
\text { \inboundscheckon } \\
\text { \plot } & -.485 & 2.6187 & -.475 & 2.0388 \\
& -.465 & 1.7320 & -.465 & 1.7320 \\
-.44 & 1.3403 & -.40 & 1.0610 \\
& -.36 & 0.9174 & -.32 & 0.8285 \\
-.27 & 0.7564 & -.22 & 0.7089 \\
-.12 & 0.6558 & 0 & 0.6366
\end{array}
\end{aligned}
$$

Note that $\mathfrak{a}(.5-.485)=2.6187, \mathfrak{a}(.5-.475)=2.0388$, and so on. The "in bounds check" feature kept $\mathrm{P}_{\mathrm{T}} \mathrm{CT}_{\mathrm{E}} \mathrm{X}$ from plotting any points with vertical coordinates greater than 2.5 . To plot the right half of $\mathfrak{a}$ the same commands were used, but with the signs of the horizontal coordinates changed to '+'.

In general, to \plot any given curve you have to provide $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}$ with a list of coordinate values, as opposed to, say, some mathematical formula.

However, you can create such a list using Fortran or $C$ or whatever, store it in a file, and have $\backslash$ plot take its input from that file.
$\mathrm{P}_{\mathrm{I}} \mathrm{CTEX}_{\mathrm{E}}$ draws lines and curves by placing lots of periods close together. This takes a lot of time, because $\mathrm{P}_{1} \mathrm{CT}_{E} \mathrm{X}$ repeatedly has to lead $\mathrm{T}_{E} \mathrm{X}$ step by simple arithmetic step through complex calculations, like finding the distance between two points in a coordinate plane, for which it has no primitives. ( $\mathrm{T}_{\mathrm{E}} \mathrm{C}$ can only do fixed point addition, subtraction, and multiplication, and division by integers.) And all those periods take up a lot of room in TEX's memory. That's the down side; the up side is that there are no restrictions on the slope of lines and the curvature of arcs. By contrast, $\mathrm{IA} \mathrm{TEX}^{2}$ 's picture environment draws lines and circles by piecing together characters from specially designed fonts. This is fast and uses little storage space, but the choice of slopes and radii is quite limited. Fortunately, this is one instance where you can have your cake and eat it too. PTCTEX knows how to use IATEX's picture objects, and $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}$ 's macros can be used inside LATEX. (Don't try this without first reading the relevant section from the $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}_{\mathrm{E}}$ manual.)

Figure 5. Diagram showing how the probabilities for the response categories I, II, III, and IV in a certain proportional hazards model vary with $\eta$. Probabilities are shown as shaded areas; higher numbered categories have greater shade density.

$\mathrm{P}_{\mathrm{I}} \mathrm{CT}_{\mathrm{E}} \mathrm{X}$ shades a region by placing a "shading symbol" at every point of a "shading lattice" that falls within the region. You have control over both the symbol and lattice. In Figure 5 three different shading lattices were used, each with a \fiverm period as the shading symbol.

Figure 6. Suicide rates in western Europe per 100,000 population per year for the years ( 19 xx ) indicated.


## Extending $\mathrm{P}_{\mathrm{T}} \mathrm{CTEX}$

Consider now how you might go about drawing Figure 6. To get started you could enter

```
\beginpicture
\setcoordinatesystem units <5pt,11pt>
\setplotarea x from 0 to 25,
    y from 0 to 0
\linethickness=.15pt
{\eightpoint \axis top
    ticks numbered from 0 to 25 by 5 / }%
\linethickness=2pt
```

These commands establish the coordinate system, draw the axis, and set $\mathrm{P}_{\mathrm{I}} \mathrm{CT}_{\mathrm{E}}$ 's line thickness parameter to 2 points for drawing the black bars. The problem that needs addressing is how to place the bars and their associated labels into the P1Cture. You could do this easily with $\mathrm{P}_{\mathrm{T}} \mathrm{CT}_{\mathrm{E}} \mathrm{X}$ 's bar graph command, or even with TEX's \halign. However the point of this section is to illustrate a technique that can often be put to good use when there isn't an upper level command that does what you want to do. Let's agree then that you have to solve this exercise using just $\mathrm{P}_{\mathrm{C}} \mathrm{CTEX}$ 's primitive commands $\backslash p u t$ and $\backslash p u t r u l e$. The most direct solution would be

```
\putrule from 0-1 to 24.1 -1
\put {Austria \sevenrm 75}
    [Br] <-5pt,-2pt> at 0-1
\putrule from 0 -2 to 23.8-2
\put {Denmark \sevenrm 73}
    [Br] <-5pt,-2pt> at 0 -2
```

and a bunch of similar commands. (The 'Br's above stand for 'baseline right' orientation.)

It would be much less tedious to enter just the bare essentials, say in the form
$\backslash$ placebars
Austria
Austria 524.1

